Form G

Rational Expressions

Simplify each rational expression. State any restrictions on the variables.

1.
$$\frac{4x+6}{2x+3}$$

3.
$$\frac{20+40x}{20x}$$

5.
$$\frac{3y^2 - 3}{y^2 - 1}$$

7.
$$\frac{x^2 + 3x - 18}{x^2 - 36}$$

Multiply. State any restrictions on the variables.

9.
$$\frac{5a}{5a+5} \cdot \frac{10a+10}{a}$$

11.
$$\frac{x^2 - 5x}{x^2 + 3x} \cdot \frac{x + 3}{x - 5}$$

13.
$$\frac{5y-20}{3y+15} \cdot \frac{7y+35}{10y+40}$$

15.
$$\frac{3x^3}{x^2-25} \cdot \frac{x^2+6x+5}{x^2}$$

Divide. State any restrictions on the variables.

17.
$$\frac{7x^4}{24y^5} \div \frac{21x}{12y^4}$$

19.
$$\frac{5y}{2x^2} \div \frac{5y^2}{8x^2}$$

21.
$$\frac{y^2 - 49}{(y - 7)^2} \div \frac{5y + 35}{y^2 - 7y}$$

23.
$$\frac{y^2 - 5y + 4}{y^2 - 1} \div \frac{y^2 - 9}{y^2 + 5y + 4}$$

8-4

Rational Expressions

- **25.** A farmer must decide whether to build a cylindrical grain silo or a rectangular grain silo. The cylindrical silo has radius r. The rectangular silo has width r and length 2r. Both silos have the same height h.
 - **a.** Write and simplify an expression for the ratio of the volume of the cylindrical silo to its surface area, including the circular floor and ceiling.
 - **b.** Write and simplify an expression for the ratio of the volume of the rectangular silo to its surface area, including the rectangular floor and ceiling.
- **c.** Compare the ratios of volume to surface area for the two silos.
- **d.** Compare the volumes of the two silos.
- **e. Reasoning** Assume the average cost of construction materials per square foot of surface area is the same for either silo. How can you measure the cost-effectiveness of each silo?

Simplify each rational expression. State any restrictions on the variables.

$$27. \ \frac{6x^2 + 5xy - 6y^2}{3x^2 - 5xy + 2y^2}$$

Multiply or divide. State any restrictions on the variables.

29.
$$\frac{x^2 - 3x - 10}{2x^2 - 11x + 5} \div \frac{x^2 - 5x + 6}{2x^2 - 7x + 3}$$

31. Open-Ended Write three rational expressions that simplify to $\frac{x+1}{x-1}$.