4-6

Practice

Form G

Completing the Square

Solve each equation by finding square roots.

1.
$$3x^2 = 75$$

2.
$$5x^2 - 45 = 0$$

3.
$$4x^2 - 49 = 0$$

4.
$$6x^2 = 216$$

5.
$$2x^2 = 14$$

6.
$$3x^2 - 96 = 0$$

7. A box is 4 in. high. Its length is 1.5 times its width. The volume of the box is 1350 in.². What are the width and length of the box?

Solve each equation.

8.
$$x^2 + 12x + 36 = 25$$

9.
$$x^2 - 10x + 25 = 144$$

10.
$$x^2 + 6x + 9 = \frac{49}{4}$$

11.
$$x^2 - 22x + 121 = 225$$

12.
$$16x^2 + 8x + 1 = 16$$

13.
$$25x^2 - 30x + 9 = 81$$

Complete the square.

14.
$$x^2 + 22x +$$

15.
$$x^2 - 30x +$$

16.
$$x^2 + 5x +$$

17.
$$x^2 - \frac{1}{2}x +$$

18.
$$25x^2 + 10x +$$

19.
$$4x^2 - 12x +$$

Solve each quadratic equation by completing the square.

20.
$$x^2 + 10x - 1 = 0$$

21.
$$x^2 + 2x - 7 = 0$$

22.
$$-x^2 + 6x + 10 = 0$$

23.
$$x^2 + 5x = 3x + 11$$

24.
$$3x^2 + 4x = 2x^2 + 3$$

25.
$$x^2 - 2x - \frac{3}{4} = 0$$

26.
$$-0.2x^2 + 0.4x + 0.8 = 0$$

27.
$$4x^2 + 20x + 1 = 0$$

Practice (continued)

Form G

Completing the Square

Rewrite each equation in vertex form.

28.
$$y = x^2 - 6x + 4$$

29.
$$y = x^2 + 14x + 50$$

30.
$$y = 3x^2 + 8x + 2$$

31.
$$y = -2x^2 + 6x - 2$$

Find the value of k that would make the left side of each equation a perfect square trinomial.

32.
$$x^2 + kx + 196 = 0$$

33.
$$64x^2 - kx + 1 = 0$$

34.
$$x^2 - kx + 16 = 0$$

35.
$$4x^2 - kx + 9 = 0$$

36.
$$16x^2 + kx + 9 = 0$$

37.
$$\frac{1}{4}x^2 - kx + \frac{1}{25} = 0$$

- **38.** The quadratic function $d = -t^2 + 4t + 33$ models the depth of water in a flood channel after a rainstorm. The time in hours after it stops raining is t and d is the depth of the water in feet.
 - **a.** Solve the equation $-t^2 + 4t + 33 = 0$.
 - **b.** Approximate the positive solution found in part (a) to two decimal places.
 - **c.** Interpret the answer to part (b) in terms of the problem.
- 39. While in orbit, a space scientist measures the pressure inside a container as it is being heated and then cooled. She records the information and discovers the pressure p, in pounds per square inch, is related to the time t in minutes after the experiment begins according to the equation $p = -0.2t^2 + 1.6t$.
 - **a.** Complete the square in the expression $-0.2t^2 + 1.6t$.
 - **b.** Rewrite the equation for p in vertex form.
 - **c.** What is a reasonable domain for this function? Explain.
 - **d.** When does the maximum pressure occur? What is the maximum pressure?