Form G

## Solving Systems Using Matrices

Identify the indicated element.

$$A = \begin{bmatrix} 3 & 5 & 8 \\ 4 & 1 & 6 \end{bmatrix}$$

$$B = \begin{bmatrix} 0 & 6 & 3 & 2 \\ 4 & 5 & 1 & 13 \\ 2 & 2 & 0 & -10 \end{bmatrix}$$

- **1.**  $A_{13}$
- **2.**  $B_{24}$

**4.**  $A_{22}$ 

- **5**. B<sub>31</sub>
- 6.  $A_{21}$
- **7.**  $B_{23}$
- **8.**  $A_{11}$

Write a matrix to represent each system.

**9.** 
$$\begin{cases} 3x + y = -4 \\ -2x + 4y = 7 \end{cases}$$

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 **10.** 
$$\begin{cases} 6x = 11 \\ -3x + 4y = 2 \end{cases}$$

11. 
$$\begin{cases} 4x - y + 2z = 10 \\ 5x + 2y - 3z = 0 \\ x - 3y + z = 6 \end{cases}$$

Write the system of equations represented by each matrix.

**12.** 
$$\begin{bmatrix} 2 & 5 & 0 & 13 \\ -3 & 1 & 2 & 6 \\ 4 & 0 & -3 & 5 \end{bmatrix}$$
 **13.** 
$$\begin{bmatrix} 2 & 1 & -7 \\ 0 & 4 & 9 \end{bmatrix}$$

**13.** 
$$\begin{bmatrix} 2 & 1 & -7 \\ 0 & 4 & 9 \end{bmatrix}$$

**14.** 
$$\begin{bmatrix} 6 & 4 & -2 & 17 \\ 1 & -5 & 2 & -10 \\ 0 & 3 & -1 & 0 \end{bmatrix}$$

Solve the system of equations using a matrix.

**15.** 
$$\begin{cases} 4x - y = 10 \\ -2x + 5y = 4 \end{cases}$$

**16.** 
$$\begin{cases} x - 2y + 3z = 18 \\ 9x + 2y - z = -2 \\ -6x - y + 2z = 4 \end{cases}$$
**17.** 
$$\begin{cases} 3x - 4y + z = 15 \\ -2x - 6y + 3z = 4 \\ 2x + 2y - 2z = -1 \end{cases}$$

17. 
$$\begin{cases} 3x - 4y + z = 15 \\ -2x - 6y + 3z = 4 \\ 2x + 2y - 2z = -1 \end{cases}$$

Form G

Practice (continued)

Solving Systems Using Matrices

**Graphing Calculator Solve each system.** 

**18.** 
$$\begin{cases} 4x + y - 2z = 3 \\ 2y + z = 4 \\ 3x - 3y - z = 9 \end{cases}$$

19. 
$$\begin{cases} 5x - 2y + z = -x - y - 2z = 5 \\ 3x + 2y + 2z = 2 \end{cases}$$

**18.** 
$$\begin{cases} 4x + y - 2z = 3 \\ 2y + z = 4 \\ 3x - 3y - z = 9 \end{cases}$$
**19.** 
$$\begin{cases} 5x - 2y + z = -1 \\ -x - y - 2z = 5 \\ 3x + 2y + 2z = 2 \end{cases}$$
**20.** 
$$\begin{cases} 3x + 5z = -4 \\ -2x + y - 3z = 9 \\ -x - 2y + 9z = 0 \end{cases}$$

- 21. Suppose the movie theater you work at sells popcorn in three different sizes. A small costs \$2, a medium costs \$5, and a large costs \$10. On your shift, you sold 250 total containers of popcorn and brought in \$1726. You sold twice as many large containers as small ones.
  - **a.** How many of each popcorn size did you sell?
  - **b.** How much money did you bring in from selling small size containers?
- 22. Open Ended Write a matrix for a system of equations that does not have a unique solution.
- 23. The following matrix shows the prices passengers on an airline flight paid for a recent ticket and how many passengers were on that flight. Some passengers paid full price for their tickets, and some bought their tickets during a half-price sale. How many passengers bought each price of ticket?

$$\begin{bmatrix}
1 & 1 & 100 \\
120 & 240 & 20,160
\end{bmatrix}$$

**24. Error Analysis** Your friend says that the matrix below represents the system of equations. What error did your friend make? What is the correct system of equations?

$$\begin{bmatrix} 4 & 0 & -1 & 4 \\ -3 & 2 & -2 & -2 \\ 1 & -3 & -2 & -6 \end{bmatrix} \qquad \begin{cases} 4x + y - z = 4 \\ -3x + 2y - 2z = -2 \\ x - 3y - 2z = -6 \end{cases}$$

$$\begin{cases} 4x + y - z = 4 \\ -3x + 2y - 2z = -2 \\ x - 3y - 2z = -6 \end{cases}$$