

PROBLEMS ON LOGIC

II.20 The negation of the converse of the statement "If $x < 0$ then $y < 0$ " is equivalent to

- (a) $y < 0$ and $x \geq 0$
- (b) $x > 0$ and $y \geq 0$
- (c) $x < 0$ or $y < 0$
- (d) If $y \leq 0$ then $x > 0$
- (e) $x < 0$ or $y \geq 0$.

III.12 Let A,B,C be statements which are either true or false. Given the hypotheses (i) if A then B and (ii) if C then B then a valid conclusion is

- (a) if C then A
- (b) if B then (A or C)
- (c) if not B then (A and C)
- (d) if (A or B) then C
- (e) if not B then not (A or C)

IV.10 Which of the following is equivalent to the statement

"If not A then (B or not C)" ?

- (a) If (not B and C) then not A
- (b) If A then (not B or C)
- (c) If (not A and B) then not C
- (d) If (not B and C) then A
- (e) If (B and not C) then A

V.14 The statement "If P then (Q and R)" is true provided

- (a) P is false and Q is false
- (b) P is true and Q is true
- (c) P is true or R is false
- (d) (P or Q) is true or R is true
- (e) (P and Q) is false and R is true

VI.18 Which is a valid conclusion to the argument whose two hypotheses are (I) If P then Q and (II) Q and not P?

- (a) P or (not Q)
- (b) P and Q
- (c) If Q then P
- (d) P or Q
- (e) P and (not Q)

VII.8 Given that the implication "If P then Q" is false,

then which of the following implications must also be false?

- (a) If Q then P
- (b) If Q then (not P)
- (c) If (P and Q) then Q
- (d) If (not P) then (P or Q)
- (e) If (not Q) then (not (P or Q))

VIII.10 If it is known that "if $y \leq 3$ then $x > z$ " then which of the following must be true?

- (a) If $x > z$ then $y \leq 3$
- (b) $y > 3$ and $x \leq z$
- (c) $y > 3$ or $x > z$
- (d) $x + 3 \geq y + z$
- (e) If $y > 3$ then $x \leq z$

IX.10 Given (I) if $x > 3$ then $y < 7$ and (II) either $x < 2$ or $y > 9$ then

- (a) $x < 2$
- (b) $y \geq 7$
- (c) $x \leq 3$
- (d) $x > y$
- (e) none of (a)-(d)

X.7 If p and q are logical statements then which of the following is always true?

- (a) if (p or q) then (if p then q)
- (b) if (p and not p) then q
- (c) if p then (p and q)
- (d) if (p or q) then q
- (e) if (if p then q) then (p or q)