Note: For each of the following questions, answer E, NOTA, means "None of the Above."

- 1.  $\lim_{h\to 0} \frac{\cos\left(\frac{\pi}{2}+h\right)}{h}$  is
  - A. 1
- B. 0
- C. -1
- D. nonexistent
- E. NOTA

- 2.  $\int_0^1 \frac{x dx}{x^2 + 1}$  is equal to
- A.  $\frac{\pi}{4}$  B.  $\ln \sqrt{2}$  C.  $\frac{1}{2}(\ln 2 1)$  D.  $\ln 2$  E. NOTA
- 3. Let  $F(x) = \int_0^x \frac{10}{1+e^t} dt$ . Which of the following statements are true?
  - I. F'(0) = 5
- II. F(2) < F(6)
- III. F is concave upward for all x.

- A. I only
- B. II only
- C. III only
- D. I and II
- E. NOTA
- 4. The base of a solid is the region bounded by the parabola  $y^2 = 4x$  and the line x = 2. Each plane section perpendicular to the x-axis is a square. The volume of the solid is
  - A. 6
- B. 8
- C. 10
- D. 16
- E. NOTA

- 5. If  $x = \sqrt{1-t^2}$  and  $y = \sin^{-1} t$ , then  $\frac{dy}{dx}$  equals
  - A.  $-\frac{\sqrt{1-t^2}}{t}$  B. -t C.  $\frac{t}{1-t^2}$

- D. 2 E. NOTA

- 6. The area of the largest isosceles triangle that can be drawn with one vertex at the origin and with the others on a line parallel to and above the x-axis and on the curve  $y = 27 - x^2$  is
  - A. 108
- B. 27 C.  $12\sqrt{3}$  D. 3
- E. NOTA

- 7.  $\int_{\pi/6}^{\pi/2} \cot x \, dx =$
- A.  $\ln \frac{1}{2}$  B.  $\ln 2$  C.  $-\ln (2 \sqrt{3})$  D.  $\ln (\sqrt{3} 1)$
- E. NOTA

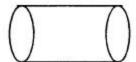
- 8. Find the slope of the curve  $r = \cos 2\theta$  at  $\theta = \frac{\pi}{6}$ .
  - A.  $\frac{\sqrt{3}}{7}$  B.  $\frac{1}{\sqrt{3}}$  C.  $\sqrt{3}$
- **D**. 0
- E. NOTA
- 9. The curve  $x^3 + x \tan y = 27$  passes through (3, 0). Use local linearization to estimate the value of y at x = 3.1. The value is

- A. -2.7 B. -0.9 C. 0 D. 0.1 E. NOTA
- 10. The coefficient of the  $x^2$  term in the Taylor polynomial for  $y = x^{2/3}$  around x = 8 is
  - A.  $-\frac{1}{144}$  B.  $-\frac{1}{72}$  C.  $-\frac{1}{9}$  D.  $\frac{1}{144}$

- E. NOTA
- 11. The equation of the tangent to the curve  $2x^2 y^4 = 1$  at the point (-1, 1) is
  - A. y = -x

- B. y = 2 x C. 4y + 5x + 1 = 0
- D. x 2y + 3 = 0
- E. NOTA

- 12. A curve is given parametrically by the equations  $x = 3 2 \sin t$  and  $y = 2 \cos t 1$ . The length of the arc from t = 0 to  $t = \pi$  is
  - A.  $\frac{\pi}{2}$
- B.  $\pi$  C. 2 +  $\pi$
- D. 2π
- E. NOTA
- 13. The only function that does not satisfy the Mean Value Theorem on the interval specified is
- A.  $f(x) = x^2 2x$  on [-3, 1] B.  $f(x) = \frac{1}{x}$  on [1, 3] C.  $f(x) = x^{2.3}$  on  $\left[\frac{1}{2}, \frac{3}{2}\right]$
- D.  $f(x) = x + \frac{1}{x}$  on [-1, 1]
- E. NOTA
- 14. A cylindrical tank is partially full of water at time t = 0, when more water begins flowing in at a constant rate. The tank becomes half full when t = 4, and is completely full when t = 12. Let h represent the height of the water at time t. During which interval is  $\frac{dh}{dt}$  increasing?
- A. 0 < t < 4 B. 0 < t < 8 C. 0 < t < 12



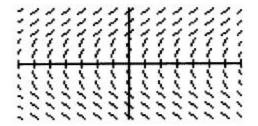
- D. 4 < t < 12 E. NOTA
- 15.  $\int_{1}^{2} \frac{dx}{\sqrt{4-x^{2}}}$  is
  - A.  $-\frac{\pi}{3}$  B.  $\frac{\pi}{6}$
- C.  $\frac{\pi}{4}$
- D.  $\frac{\pi}{3}$
- E. NOTA

- 16. The area inside  $r = 3 \sin \theta$  and outside  $r = 1 + \sin \theta$  is given by
  - A.  $\int_{\pi/2}^{\pi/2} \left[ 9\sin^2\theta (1+\sin\theta)^2 \right] d\theta$ 
    - B.  $\int_{-\pi}^{\pi/2} (2\sin\theta 1)^2 d\theta$

  - C.  $\frac{1}{2} \int_{\pi/6}^{5\pi/6} (8\sin^2\theta 1) d\theta$  D.  $\frac{9\pi}{4} \frac{1}{2} \int_{\pi/6}^{5\pi/6} (1 + \sin\theta)^2 d\theta$
- E. NOTA

- 17.  $\lim_{x\to\infty} x^{1/x}$  is
  - A. 0
- B. 1
- C. e
- D. ∞
- E. NOTA

18. Which equation has the slope field shown below?



- A.  $\frac{dy}{dx} = \frac{5}{y}$  B.  $\frac{dy}{dx} = \frac{5}{x}$  C.  $\frac{dy}{dx} = \frac{x}{y}$  D.  $\frac{dy}{dx} = 5y$  E. NOTA

- 19. Suppose the function f is both increasing and concave up on [a, b]. Then, using the same number of subdivisions, and with L, R, M, and T denoting respectively Left, Right, Midpoint, and Trapezoid sums, it follows that
  - A.  $R \le T \le M \le L$
- B.  $R \le M \le T \le L$  C.  $L \le T \le M \le R$

- D.  $L \le M \le T \le R$
- E., NOTA
- 20. Let  $\int_{0}^{x} f(t)dt = x \sin \pi x$ . Then f(3) =

- A.  $-3\pi$  B. -1 C. 1 D.  $3\pi$
- E. NOTA

- 21. If f'(x) = 2f(x) and f(2) = 1, then f(x) =

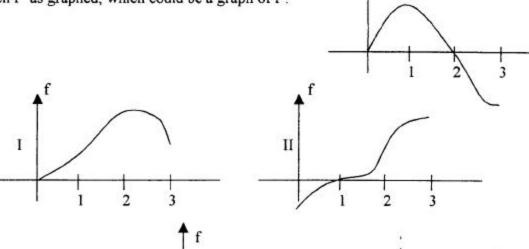
  - A.  $e^{2x-4}$  B.  $e^{2x} + 1 e^4$  C.  $e^{4-2x}$  D.  $e^{2x+1}$
- E. NOTA

22. 
$$\int_0^6 f(x-1)dx =$$

- A.  $\int_{-1}^{7} f(x) dx$  B.  $\int_{-1}^{5} f(x) dx$  C.  $\int_{-1}^{7} f(x+1) dx$  D.  $\int_{1}^{7} f(x) dx$
- E. NOTA
- 23. Let  $f(x) = x^5 + 1$  and let g be the inverse function of f. What is the value of g'(0)?
  - A -1

- B. 1 C.  $\frac{1}{5}$  D. g'(0) does not exist
- E. NOTA

24. Given f' as graphed, which could be a graph of f?



- A. I only
- B. II only

III

- C. III only
- D. I and III
- E. NOTA
- 25. A particle moves on a straight line so that its velocity at time t is given by v = 4s, where s is its distance from the origin. If s = 3 when t = 0, then, when  $t = \frac{1}{2}$ , s equals
  - A.  $1 + e^2$  B.  $2e^3$  C.  $e^2$  D.  $2 + e^2$

- E. NOTA

- 26. The first quadrant region bounded by  $y = \frac{1}{\sqrt{r}}$ , y = 0, x = q (0 < q < 1), and x = 1 is rotated about the x-axis. The volume obtained as q → 0<sup>+</sup> equals

  - A  $\frac{2\pi}{3}$  B.  $\frac{4\pi}{3}$  C.  $2\pi$  D.  $4\pi$  E. NOTA

- 27. The area of the surface generated by revolving the curve  $y = \sin x$  from x = 0 to  $x = \pi$  about the x-axis is
  - A.  $2\pi \left(\sqrt{2} + \ln\left(1 + \sqrt{2}\right)\right)$  B.  $2\pi + \ln\left(1 + \sqrt{2}\right)$  C.  $2\pi + \frac{1}{2}\ln 2$

- D.  $2^{3/2}(\pi + \ln 2)$
- E. NOTA
- 28. The interval of convergence of  $\sum_{n=1}^{\infty} nx^n$  is

- A. (-1, 1) B. [-1, 1) C. (-1, 1] D. [-1, 1]
- E. NOTA

- 29. Which of the following series converges?

- A.  $\sum \frac{1}{\sqrt[3]{n}}$  B.  $\sum \frac{1}{\sqrt{n}}$  C.  $\sum \frac{1}{n}$  D.  $\sum \frac{1}{10n-1}$
- E. NOTA

- $30. \int \frac{x^2 + 2}{x^2 + 2x} dx =$
- A.  $\ln |x| + C$  B.  $\ln |x| 3 \ln |x + 2| + C$  C.  $\frac{x^3}{3} \ln |x| + 2 \ln |x + 2| + C$
- D.  $\ln \left| \frac{x}{(x+2)^3} \right| + x + C$
- E. NOTA